F-strings

Put f in front of string, any valid Python expression goes inside curly brackets.

```
>>> greeting = 'Ahoy'
>>> noun = 'Boat'
>>> f"{greeting}, {noun.upper()}y{noun}Face"
'Ahoy, BOATyBoatFace'
>>> f"{greeting*3}, {noun[0:3]}y{noun[-1]}Face"
'AhoyAhoyAhoy, BoaytFace'
```

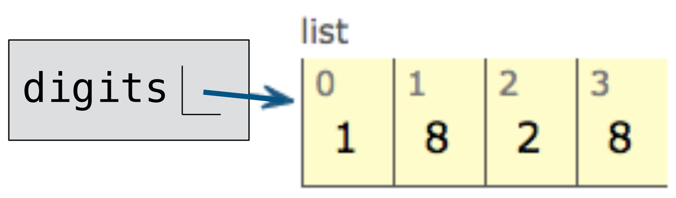
Parts of a Traceback:

- The error message itself
- Line #s on the way to the error
- What's on those lines

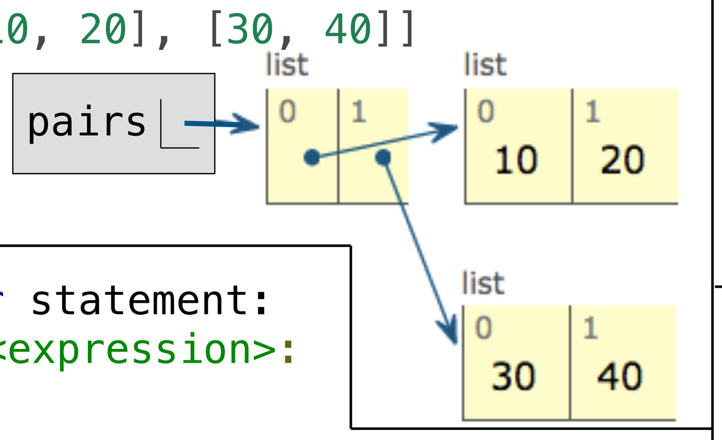
```
Traceback (most recent call last):
    File "main.py", line 14, in <module>
        quot3 = div_numbers(10, 0)
    File "main.py", line 10, in div_numbers
        return dividend/divisor
ZeroDivisionError: division by zero
```

Lists:

```
>>> digits = [1, 8, 2, 8]
>>> len(digits)
4
>>> digits[3]
8
```




```
>>> [2, 7] + digits * 2
[2, 7, 1, 8, 2, 8, 1, 8, 2, 8]

>>> pairs = [[10, 20], [30, 40]]
>>> pairs[1]
[30, 40]
>>> pairs[1][0]
30
```



Executing a for statement:

```
for <name> in <expression>:
    <suite>
```

1. Evaluate the header <expression>, which must yield an iterable value (a list, tuple, iterator, etc.)
2. For each element in that sequence, in order:
   - A. Bind <name> to that element in the current frame
   - B. Execute the <suite>

Unpacking in a for statement: (A sequence of fixed-length sequences)

```
>>> pairs=[[1, 2], [2, 2], [3, 2], [4, 4]]
>>> same_count = 0
```

(A name for each element in a fixed-length sequence)

```
>>> for x, y in pairs:
...     if x == y:
...         same_count = same_count + 1
>>> same_count
2
```

..., -3, -2, -1, 0, 1, 2, 3, 4, ...

range(-2, 2)

Length: ending value - starting value
Element selection: starting value + index

```
>>> list(range(-2, 2))
[-2, -1, 0, 1]
```

(List constructor)

```
>>> list(range(4))
[0, 1, 2, 3]
```

(Range with a 0 starting value)

Membership:

```
>>> digits = [1, 8, 2, 8]
>>> 2 in digits
True
>>> 1828 not in digits
True
```

Slicing:

```
>>> digits[0:2]
[1, 8]
>>> digits[1:]
[8, 2, 8]
```

(Slicing creates a new object)

Identity:
<exp0> is <exp1>
evaluates to True if both <exp0> and <exp1> evaluate to the same object
Equality:
<exp0> == <exp1>
evaluates to True if both <exp0> and <exp1> evaluate to equal values
Identical objects are always equal values

List comprehensions:

[<map exp> for <name> in <iter exp> if <filter exp>]

Short version: [<map exp> for <name> in <iter exp>]

A combined expression that evaluates to a list using this evaluation procedure:
1. Add a new frame with the current frame as its parent
2. Create an empty *result list* that is the value of the expression
3. For each element in the iterable value of <iter exp>:
   - A. Bind <name> to that element in the new frame from step 1
   - B. If <filter exp> evaluates to a true value, then add the value of <map exp> to the result list

Dictionaries:

```
words = {
        "más": "more",
        "otro": "other",
        "agua": "water"
}

>>> len(words)
3
>>> "agua" in words
True
>>> words["otro"]
'other'
>>> words["pavo"]
KeyError
>>> words.get("pavo", "🤔")
'🤔'
```

Dictionary comprehensions:

{key: value for <name> in <iter exp>}

```
>>> {x: x*x for x in range(3,6)}
{3: 9, 4: 16, 5: 25}

>>> [word for word in words]
['más', 'otro', 'agua']
>>> [words[word] for word in words]
['more', 'other', 'water']
>>> words["oruguita"] = 'caterpillar'
>>> words["oruguita"]
'caterpillar'
>>> words["oruguita"] += '🐛'
>>> words["oruguita"]
'caterpillar🐛'
```

Functions that aggregate iterable arguments

- **sum**(iterable[, start]) -> value — *sum of all values*
- **max**(iterable[, key=func]) -> value — *largest value*
  max(a, b, c, ...[, key=func]) -> value
  min(iterable[, key=func]) -> value — *smallest value*
  min(a, b, c, ...[, key=func]) -> value
- **all**(iterable) -> bool — *whether all are true*
  any(iterable) -> bool — *whether any is true*

Many built-in Python sequence operations return iterators that compute results lazily

map(func, iterable):
  Iterate over func(x) for x in iterable
filter(func, iterable):
  Iterate over x in iterable if func(x)
zip(first_iter, second_iter):
  Iterate over co-indexed (x, y) pairs
reversed(sequence):
  Iterate over x in a sequence in reverse order

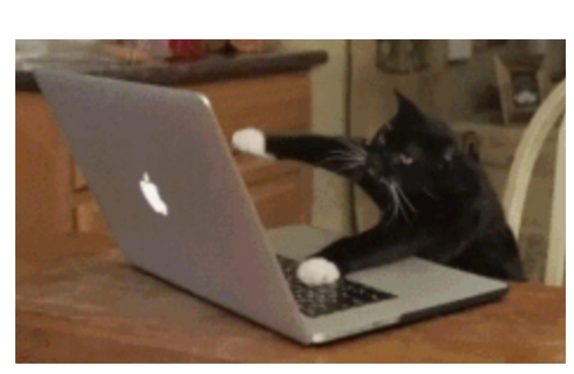
To view the contents of an iterator, place the resulting elements into a container

list(iterable):
  Create a list containing all x in iterable
tuple(iterable):
  Create a tuple containing all x in iterable
sorted(iterable):
  Create a sorted list containing x in iterable

```
def cascade(n):
    if n < 10:
        print(n)
    else:
        print(n)
        cascade(n//10)
        print(n)

>>> cascade(123)
123
12
1
12
123
```

```
          n: 0, 1, 2, 3, 4, 5, 6,  7,  8,
 virfib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,

def virfib(n):
  if n == 0:
    return 0
  elif n == 1:
    return 1
  else:
    return virfib(n-2) + virfib(n-1)
```

Exponential growth. E.g., recursive fib Incrementing *n* multiplies *time* by a constant	$\Theta(b^n)$	$O(b^n)$
Quadratic growth. E.g., overlap Incrementing *n* increases *time* by *n* times a constant	$\Theta(n^2)$	$O(n^2)$
Linear growth. E.g., slow exp Incrementing *n* increases *time* by a constant	$\Theta(n)$	$O(n)$
Logarithmic growth. E.g., exp_fast Doubling *n* only increments *time* by a constant	$\Theta(\log n)$	$O(\log n)$
Constant growth. Increasing *n* doesn't affect time	$\Theta(1)$	$O(1)$



List mutation:

```
>>> a = [10]
>>> b = a
>>> a == b
True
>>> a.append(20)
>>> a == b
True
>>> a
[10, 20]
>>> b
[10, 20]
```

```
>>> a = [10]
>>> b = [10]
>>> a == b
True
>>> b.append(20)
>>> a
[10]
>>> b
[10, 20]
>>> a == b
False
```

You can **copy** a list by calling the list constructor or slicing the list from the beginning to the end.

```
>>> a = [10, 20, 30]
>>> list(a)
[10, 20, 30]
>>> a[:]
[10, 20, 30]
```

Tuples:

```
>>> empty = ()
>>> len(empty)
0
>>> conditions = ('rain', 'shine')
>>> conditions[0]
'rain'
>>> conditions[0] = 'fog'
Error
```

```
>>> all([False, True])
False
>>> all([])
True
>>> sum([1, 2])
3
>>> sum([1, 2], 3)
6
>>> sum([])
0
>>> sum([[1], [2]], [])
[1, 2]
```

```
>>> any([False, True])
True
>>> any([])
False
>>> max(1, 2)
2
>>> max([1, 2])
2
>>> max([1, -2], key=abs)
-2
```

List methods:

```
>>> suits = ['coin', 'string', 'myriad']
>>> suits.pop()               # Remove and return the last element
'myriad'
>>> suits.remove('string')    # Removes first matching value
>>> suits.append('cup')
>>> suits.extend(['sword', 'club'])   # Add all values
>>> suits[2] = 'spade'
>>> suits
['coin', 'cup', 'spade', 'club']
>>> suits[0:2] = ['diamond']  # Replace a slice with values
>>> suits
['diamond', 'spade', 'club']
>>> suits.insert(0, 'heart')  # Add an element at an index
>>> suits
['heart', 'diamond', 'spade', 'club']
```

Truthiness & falsiness:

False values:
- Zero
- False
- None
- An empty string, list, dict, tuple

All other values are true values.

```
>>> bool(0)
False
>>> bool(1)
True
>>> bool('')
False
>>> bool('0')
True
>>> bool([])
False
>>> bool([[]])
True
>>> bool({})
False
>>> bool(())
False
>>> bool(lambda x: 0)
True
```

Conditional expressions:

<consequent> if <predicate> else <alternative>

x if x > 0 else 0

iter(iterable):
  Return an iterator over the elements of an iterable value
next(iterator):
  Return the next element

```
>>> s = [3, 4, 5]
>>> t = iter(s)
>>> next(t)
3
>>> next(t)
4
```

```
>>> d = {'one': 1, 'two': 2, 'three': 3}
>>> k = iter(d)
>>> next(k)
'one'
>>> next(k)
'two'
>>> v = iter(d.values())
>>> next(v)
1
>>> next(v)
2
```

A generator function is a function that ***yield****s values instead of* ***return****ing.*

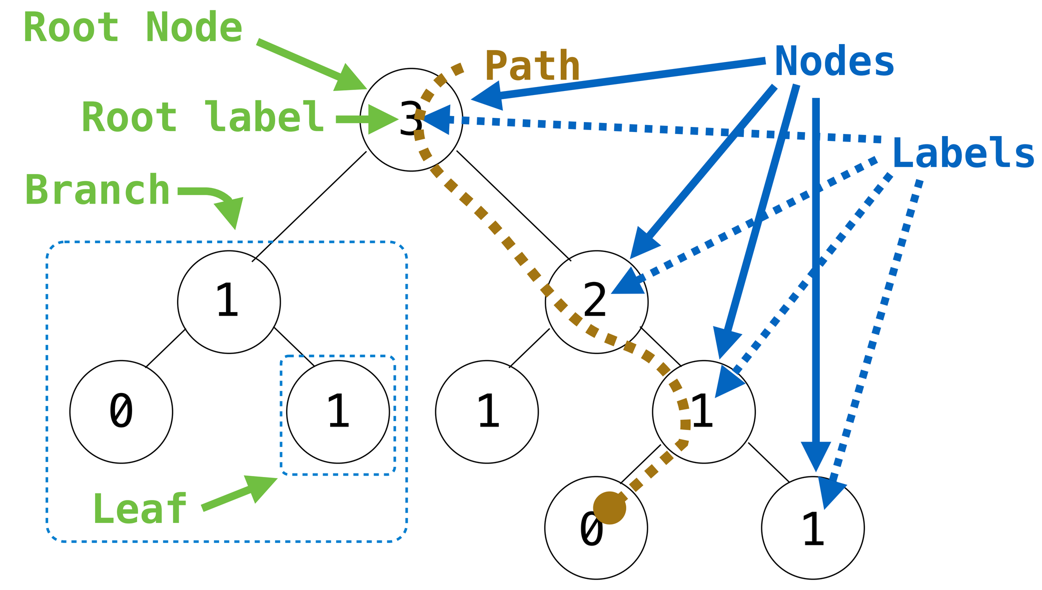
```
def plus_minus(x):
    yield x
    yield -x

>>> t = plus_minus(3)
>>> next(t)
3
>>> next(t)
-3
```

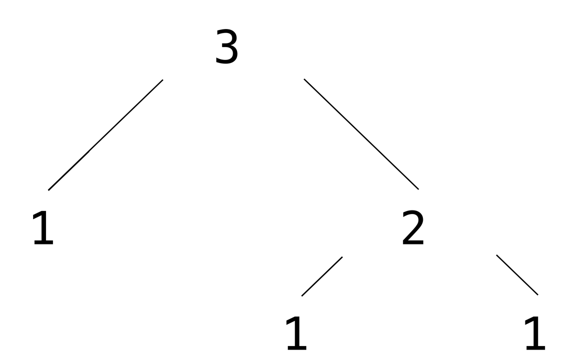
```
def a_then_b(a, b):
    yield from a
    yield from b

>>> list(a_then_b([3, 4], [5, 6]))
[3, 4, 5, 6]
```

```
def countdown(k):
    if k > 0:
        yield k
        yield from countdown(k - 1)

>>> c = countdown(3)
>>> next(c)
3
>>> next(c)
2
>>> next(c)
1
```

Recursive description:
- A **tree** has a root **label** and a list of **branches**
- Each branch is a **tree**
- A tree with zero branches is called a **leaf**

Relative description:
- Each location in a tree is a **node**
- Each **node** has a **label**
- One node can be the **parent/child** of another





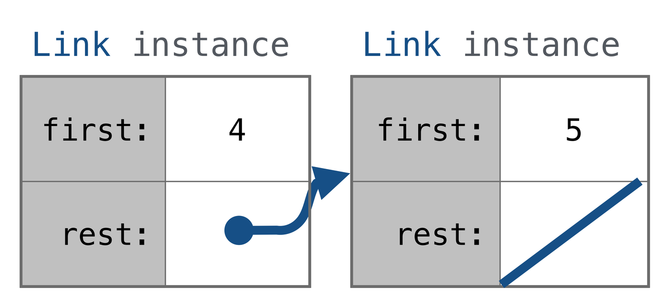

```
>>> Tree(3, [Tree(1),
...          Tree(2, [Tree(1),
...                   Tree(1)])])

def fib_tree(n):
    if n == 0 or n == 1:
        return Tree(n)
    else:
        left = fib_Tree(n-2)
        right = fib_Tree(n-1)
        fib_n = left.label+right.label
        return Tree(fib_n,[left, right])
```

```
class Tree:
    def __init__(self, label, branches=[]):
        self.label = label
        for branch in branches:
            assert isinstance(branch, Tree)
        self.branches = list(branches)

    def is_leaf(self):
        return not self.branches

def leaves(tree):
    "The leaf values in a tree."
    if tree.is_leaf():
        return [tree.label]
    else:
        return sum([leaves(b) for b in tree.branches], [])
```

Built-in isinstance function: returns True if branch has a class that *is* **or** *inherits from* Tree

```
class Link:
    empty = ()

    def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance(rest, Link)
        self.first = first
        self.rest = rest

    def __repr__(self):
        if self.rest:
            rest = ', ' + repr(self.rest)
        else:
            rest = ''
        return 'Link('+repr(self.first)+rest+')'

    def __str__(self):
        string = '<'
        while self.rest is not Link.empty:
            string += str(self.first) + ' '
            self = self.rest
        return string + str(self.first) + '>'
```

Some zero length sequence




```
>>> s = Link(4, Link(5))
>>> s
Link(4, Link(5))
>>> s.first
4
>>> s.rest
Link(5)
>>> print(s)
<4 5>
>>> print(s.rest)
<5>
>>> s.rest.rest is Link.empty
True
```

The result of calling **repr** on a value is what Python prints in an interactive session

The result of calling **str** on a value is what Python prints using the **print** function

```
>>> 12e12
12000000000000.0
>>> print(repr(12e12))
12000000000000.0
```

```
>>> today = datetime.date(2019, 10, 13)
>>> print(today)
2019-10-13
```

str and **repr** are both polymorphic; they apply to any object

repr invokes a zero-argument method __repr__ on its argument

```
>>> today.__repr__()
'datetime.date(2019, 10, 13)'
>>> today.__str__()
'2019-10-13'
```

Anatomy of a recursive function:
- The **def statement header** is like any function
- Conditional statements check for **base cases**
- Base cases are evaluated **without recursive calls**
- Recursive cases are evaluated **with recursive calls**

```
def sum_digits(n):
  "Sum the digits of positive integer n."
  if n < 10:
     return n
  else:
     all_but_last, last = n // 10, n % 10
     return sum_digits(all_but_last) + last
```

- **Recursive decomposition**: finding simpler instances of a problem.
- E.g., count_partitions(6, 4)
- Explore two possibilities:
  - Use at least one 4
  - Don't use any 4
- Solve two simpler problems:
  - count_partitions(2, 4)
  - count_partitions(6, 3)
- Tree recursion often involves exploring different choices.

```
def count_partitions(n, m):
    if n == 0:
        return 1
    elif n < 0:
        return 0
    elif m == 0:
        return 0
    else:
        with_m = count_partitions(n-m, m)
        without_m = count_partitions(n, m-1)
        return with_m + without_m
```

Python object system:

Idea: All bank accounts have a **balance** and an account **holder**; the **Account** class should add those attributes to each of its instances

A new instance is created by calling a class

```
>>> a = Account('Jim')
>>> a.holder
'Jim'
>>> a.balance
0
```

An account instance

balance: 0	holder: 'Jim'

When a class is called:
1. A new instance of that class is created:
2. The __init__ method of the class is called with the new object as its first argument (named self), along with any additional arguments provided in the call expression.

__init__ is called a constructor

self should always be bound to an instance of the Account class or a subclass of Account

```
class Account:
    def __init__(self, account_holder):
        self.balance = 0
        self.holder = account_holder
    def deposit(self, amount):
        self.balance = self.balance + amount
        return self.balance
    def withdraw(self, amount):
        if amount > self.balance:
            return 'Insufficient funds'
        self.balance = self.balance - amount
        return self.balance
```

Function call: all arguments within parentheses

```
>>> type(Account.deposit)
<class 'function'>
>>> type(a.deposit)
<class 'method'>
```

Method invocation: One object before the dot and other arguments within parentheses

```
>>> Account.deposit(a, 5)
10
>>> a.deposit(2)
12
```

Call expression

Dot expression

<expression> . <name>

The <expression> can be any valid Python expression.
The <name> must be a simple name.
Evaluates to the value of the attribute looked up by <name> in the object that is the value of the <expression>.

To evaluate a dot expression:
1. Evaluate the <expression> to the left of the dot, which yields the object of the dot expression
2. <name> is matched against the instance attributes of that object; if an attribute with that name exists, its value is returned
3. If not, <name> is looked up in the class, which yields a class attribute value
4. That value is returned unless it is a function, in which case a bound method is returned instead

Assignment statements with a dot expression on their left-hand side affect attributes for the object of that dot expression
- If the object is an instance, then assignment sets an instance attribute
- If the object is a class, then assignment sets a class attribute

Account class attributes

interest: ~~0.02~~ ~~0.04~~ 0.05 (withdraw, deposit, __init__)

Instance attributes of jim_account

balance: 0 holder: 'Jim' interest: 0.08

Instance attributes of tom_account

balance: 0 holder: 'Tom'

```
>>> jim_account = Account('Jim')
>>> tom_account = Account('Tom')
>>> tom_account.interest
0.02
>>> jim_account.interest
0.02
>>> Account.interest = 0.04
>>> tom_account.interest
0.04
>>> jim_account.interest
0.04
```

```
>>> jim_account.interest = 0.08
>>> jim_account.interest
0.08
>>> tom_account.interest
0.04
>>> Account.interest = 0.05
>>> tom_account.interest
0.05
>>> jim_account.interest
0.08
```

```
class CheckingAccount(Account):
    """A bank account that charges for withdrawals."""
    withdraw_fee = 1
    interest = 0.01
    def withdraw(self, amount):
        return Account.withdraw(self, amount + self.withdraw_fee)
                                     or
        return super().withdraw(     amount + self.withdraw_fee)
```

To look up a name in a class:
1. If it names an attribute in the class, return the attribute value.
2. Otherwise, look up the name in the base class, if there is one.

```
>>> ch = CheckingAccount('Tom')  # Calls Account.__init__
>>> ch.interest     # Found in CheckingAccount
0.01
>>> ch.deposit(20)  # Found in Account
20
>>> ch.withdraw(5)  # Found in CheckingAccount
14
```